Axillary nodal prognostic impact of two-dimensional tumor heterogeneity flux in breast cancer: evaluation via dynamic contrast-enhanced magnetic resonance imaging

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Background: Breast cancer remains to have a high mortality toll in women worldwide. Several studies indicate benefit in identifying axillary nodal involvement towards effective patient risk stratification and treatment. Tumor heterogeneity recently emerged as a key factor impacting clinical outcomes. Voxel intensity gradient (VIG), a measure of contrast amongst radiological features of heterogeneity, harbors significance in determining intra-tumoral properties. Our project aims to apply the divergence theorem in correlating the 2-dimensional (2D) surface flux of this quantity to extra-tumoral axillary nodal involvement.

Methods: A retrospective cohort of 47 patients with early stage breast cancer following surgery was accrued. Pathology information and preoperative dynamic contrast enhanced magnetic resonance imaging (DCE-MRI) sequences were acquired. Tumor volumes were contoured and exported in slices for digital delineation, filtration, and computation. VIG and VIG divergence were approximated at every tumor pixel and divergence structurally summed. This measure of flux was normalized to tumor volume. Statistical analysis utilized Pearson and Spearman correlation coefficients with leave-one-out (LOO) cross validation.

Results: Among the 47 patients analyzed, 33 had T1 tumors with size (1.02±0.48 cm) and 14 had T2 tumors (3.10±0.86 cm). Normalized heterogeneity flux demonstrated significant correlation with axillary nodal ratio of positive to number collected: for non-sentinel ratio r=0.57 (P=0.001), and total node ratio r=0.50 (P<0.001). In nodal-positive patients r=0.72 (P=0.001) and r=0.58 (P=0.002), respectively. All mean squared errors were <0.05.

Conclusions: In quantifying heterogeneity departing the surface, flux mechanistically exhibited correlation with axillary nodal involvement. This correlation is optimally displayed in patients with nodal positivity. This novel radiological variable capable of characterizing tumor environment may be incorporated into future prognostic indices (nomograms) aimed at helping clinicians with axillary risk assessment.

Keywords: Breast cancer; heterogeneity; radiological analysis; magnetic resonance imaging (MRI)

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Introduction

Tumor heterogeneity

The absence of uniformity in certain features characterizing a cancer is referred to as tumor heterogeneity. This property may be described at various stages ranging from molecular and genetic to phenotypic and structural (1,2). The evaluation of heterogeneity may thus include methodologies as biological assays, histological reviews, radiological imaging and theoretical models amongst others (3-6). Extensive work in these areas elucidated several clinical ramifications associated with greater degrees of heterogeneity in tumors. This is particularly valid in breast cancer, where assessment of heterogeneity yields estimations regarding prognostic factors and guides therapeutics (7,8).

Radiological modalities and features

In harboring first, second, and higher order statistics, mined radiological data may be incorporated with clinical data in formulating models to enhance diagnostic, prognostic, and predictive capacities (9). Different imaging modalities as magnetic resonance imaging (MRI), positron emission tomography (PET) and others have been studied in assessing tumor heterogeneity (10,11). Such radiological applications allowed for delineation of an array of texture analysis parameters eligible for quantifying tumor heterogeneity (12). Development of such parameters allowed systemic classification under orders pertaining to the degree of inter-voxel relationships assessed (13). First order variables generally provide composite measures of voxel intensities as a mean, median, standard deviation, etc. Second order variables, including adjacent contrast and entropy, account for the spatial configuration of a set of voxels and gauge relative conditions. Third order variables, including coarseness, busyness, and complexity, display sensitivity for finer relationships through local cluster or neighborhood analysis of grayscale variation (13).

The voxel intensity gradient (VIG) is a second-order contrast-parameter quantifying the directional variation in intensity values amongst adjacent voxels (12). Granted a population of voxels comprising a digitalized structure, this gradient may be computed for each member through consideration of its neighboring elements. The biological manifestations of voxel intensities on dynamic contrast-enhanced (DCE-) MRI include vascular components, with greater values implicating enhanced containment of Gadolinium based radiocontrast agent (14,15). Such adroit localization of contrast is specific to developed vessels in breast cancer, as confirmed in patients and animal models (16,17). Thus spatial regions encompassing the highest variation of voxel intensities, or greatest VIG, are mechanistically linked to harboring augmented angiogenesis. Special care must be implemented in the filtering and exclusion of mature vessels distinct from tumor parenchyma nesting within the structure. Breast DCE-MRI images are capable of undergoing processing via digital algorithms in detecting these vessels (18). MRI further displays exceptional resolution and tissue differentiation in breast cancer, making it suitable as the ideal modality in our study (16,19).

Divergence theorem and boundary analysis

VIG has been evaluated and correlated with clinical outcomes in various categories of cancer (20,21). Unfortunately, the majority of studies investigating these parameters and their biological representations yield results pertaining exclusively to the tumor volume in contrast to its surface. One reason is the presence of more physical voxels and data available for analysis. A second reason is the intrinsic difficulty in gauging dynamics at the tumor surface provided a temporally static image. A certain relationship generating information regarding the surface of an object given measures acquired within its volume is the divergence theorem. It is also referred to as Gauss’s theorem, when applied to a three-dimensional closed surface, and Green’s theorem. It demonstrates application to fields in mathematics, physics and engineering, including radiological analyses (22). The divergence theorem assesses the sum of a vector field’s divergence over an enclosed surface and equates it to the total flux of this field through the boundary of this space. The three-dimensional general form appears as:

\[
\oint_{\partial V} \mathbf{f} \cdot d\mathbf{s} = \int_{V} \left( \nabla \cdot \mathbf{f} \right) dV \tag{1}
\]

Assessment of axillary nodal status

Impactful clinical trials have demonstrated momentous value in identifying breast cancer patients at high-risk for axillary nodal involvement (23,24). The burden of axillary involvement influences staging and management of patients. Previous investigations have shed light on such risk in different breast cancer cohorts utilizing non-invasive techniques as imaging or molecular assays
In evaluating measures of tumor heterogeneity flux, our project aims to enhance current predictive capabilities regarding metastatic spread to axillary nodes in early stage breast cancer patients. To this effect, our project will model the VIG as a temporally-independent spatial vector field defined in the tumor region described on DCE-MRI in early stage breast cancer patients. The focus on spatial resolution is merited since morphological architecture, which defines the respective VIG field, in addition to DCE signal intensity time course patterns were shown to be preserved given a sacrifice in temporal kinetic information (29). The field will be representative of the degree of radiological heterogeneity inherent to the tumor. Overall objectives involve computing the summated divergence of this VIG field, and employing the divergence theorem to obtain the volume normalized flux of this heterogeneity marker. Pathological records corresponding to the respective tumors will be referenced in formulating prognostic correlations of this novel heterogeneity measure to extra-tumoral axillary nodal status.

\[
\bar{f} = \text{VIG} = \nabla I
\]

\[
\int_{\partial \Omega} \bar{f} \cdot d\Sigma = \int \left( \nabla \cdot \bar{f} \right) dV
\]

Methods

Project framework

Information derived from patient records was incorporated into a secure database established using the institutionally provided online project manager Research Electronic Data Capture REDCap™ (Vanderbilt, Nashville, TN). Consistent compliance in accordance with standards set by HIPAA was enforced through regulation of access rights via the departmental IT branch. Design and implementation of the project was subject to departmental board review and approval. Participants included in the study provided prior informed consent with respect to anonymous data collection and utilization.

Pathological review

A retrospective extraction of pertinent patient data was performed using the University of Miami Electronic Medical Record system. A filtered list of breast cancer patients at the Sylvester Comprehensive Cancer Center allowed for consequential patient accrual. Such patients underwent adjuvant radiation therapy between 2006 and 2015 typically with additional adjuvant chemotherapy or hormonal therapy. Study inclusion criteria necessitate a diagnosis of early stage breast cancer, defined as either T1 or T2 staging through clinical or pathological assessment with clinical nodal-negativity in accordance with the American Joint Committee on Cancer 7th edition classification (30). Inclusion criteria involved patients harboring pathologic N0, N1, and N2 disease. Patients receiving neoadjuvant systemic therapy or surgery prior to their breast MRI were excluded from inclusion. The study group was comprised of 47 women who met the criteria of early stage breast cancer with pre-treatment evaluation via breast MRI. Among the 47 patients analyzed, 33 had T1 tumors and 14 had T2 tumors. Pathologically measured tumor size (mean ± standard deviation) was 1.02±0.48 cm and 3.10±0.86 cm for T1 and T2, respectively. Median age was 54 years ranging from 40 to 85 years. Post-menopausal state was determined on 27 patients (57.4%) and pre-menopausal state on 8 patients (17.0%). Surgical pathology interpretations were acquired by reviewing official reports issued by board-certified pathologists (with 15–20 years of experience in breast pathology interpretation) at the University of Miami. In particular, relevant data identified included the ratio of positive axillary lymph nodes to total number sampled, in addition to tumor size, grade, receptor status, lymphovascular space invasion, and extracapsular extension.

Image acquisition

MRI radiological sequences were obtained at the University of Miami for 41/47 (87.2%) patients while 6/47 patients (12.8%) attained outside imaging. Every patient was uniformly scanned at a 1.5 Tesla field: institutionally, thirty-eight patients were scanned at Magnetom Sonata™ (Siemens, Erlangen, Germany) and outside studies were carried out on Siemens Espree™ (n=2), Siemens Avanto™ (n=2) and Signa HDxt™ (n=2) (GE, Waukesha, USA). The acquisition protocol criteria required a systematic generation of DCE-MRI sequences on a 1.5 Tesla magnet using dedicated breast coils with a mean TR time of 4.3 ms and TE time of 1.51 ms. Axial T1, T2 and inversion recovery sequences were performed. Subsequently, T1, 3-D volume acquisition was obtained using multiple frames in dynamic fashion before and after Gadoteridol (ProHance®, Bracco Imaging, Milan, Italy) administration intravenously at a dose of 0.1 mmol/kg at a rate of 10–60 cc/min.
DynaCAD was used for further evaluation of images and performance of specialized curves and analysis of contrast uptake. Maximum intensity projections, subtracted image sets, and 3-D reconstructions were also obtained. Mean voxel resolutions were 0.417x0.417x1.35 mm (0.235 mm³), with mean image data matrices of size 768x768x112 pixels. The imaging protocol used was in accordance with American College of Radiology guidelines.

**Radiological algorithm**

Analysis of MRI studies was performed utilizing commercially available software MIM™ (MIM Vista Corp, Cleveland, OH). All imaging DCE-MRI sequences were uploaded in MIM and viewed in three orientations (Figure 1A). The tumor was outlined by a board certified, fellowship trained breast radiologist with 14 years of experience and/or radiation oncologist on the DCE-MRI series. The images were exported using MIM as a series of 2-dimensional (2D) slices in .TIFF format. This format was elected to standardize analysis of all axial slices between patients to ensure consistency and accuracy in the 2D computations. Further, a lack of compression allows .TIFF images to forego original data loss and retain compatibility with processing software. This series was processed in the GNU Image Manipulation Program (GIMP) to filter out image components not relevant to displaying the tumor and equalize dimensions of each file (Figure 1B). GIMP was used to superimpose a pure blue background (hexadecimal code #0000ff) saved upon each slice as a copy for tumor delineation and identification by other software (Figure 1C). Mature vessels not pertaining to tumor parenchyma were detected using a RGB intensity threshold of 0.2 relative to unity and excluded. Code scripts pertaining to image series importation, tumor recognition (Figure 1D), mature vessel filtration (Figure 1E) and relevant computations were composed and compiled using commercially available Mathematica™ (Wolfram Research, Champaign, IL, USA).

The VIG ($\nabla V$) was modeled as the vector field of interest in our analysis. It was approximated in 2-dimensions for each pixel $(i)$ with coordinates $(x,y)$ encompassed by our tumor perimeter on every 2D axial slice. This was performed by averaging the grayscale values of the two adjacent pixels $(x\pm\Delta x, y)$ in one dimension and summing it with the result from repeating this operation in the orthogonal direction $(x,y\pm\Delta y)$. In particular, the pixels one column and row behind the element of interest were subtracted from those one column and row ahead. Grayscale values for each pixel were obtained via the mean of the three red, green, and blue (RGB) components characterizing the pixel. Pixels with adjacent elements falling on or exterior to the border were excluded. A 2D matrix spanning the image length and width was populated with values corresponding to the VIG at each tumor pixel $[I'(x,y)]$. Non-tumor pixels carried a null placeholder. This operation was again applied to the VIG in ascertaining the divergence of the gradient at each pixel $[\nabla \cdot \nabla I']$. A new 2D matrix was constructed harboring the divergence values at the respective element locations for each transverse slice. Granted each pixel is identical in length and width $(\Delta x=\Delta y)$, its area is equal to a side squared $(\Delta A=\Delta x^2)$. Since each divergence term carries an inverted squared relationship to a pixel side $[\nabla \cdot \nabla I'] = \frac{\nabla I'(x,y)}{\Delta A}$, this cancels the element of area incorporated into the sum. Thus, a summation was performed over all non-null values contained in the divergence matrix disregarding dimensional factors. Further computing the series across all slices is representative of the integration of divergence over the tumor’s volume in the divergence theorem. This output was normalized to the total volume of the tumor $(V)$, calculated from the primary contour. This quantity thus approximates the surface flux of the VIG heterogeneity $(\Phi_v)$ normalized per unit tumor volume $(\Phi_v/V)$.

$\nabla V (x,y) \approx I' (x,y)$

$$\begin{align*}
\nabla V (x,y) &= I' (x,y) \\
&= I (x+\Delta x,y) - I (x, y) \\
&\quad + I (x,y+\Delta y) - I (x,y) \\
&\quad + I (x+\Delta x,y+\Delta y) - I (x,y+\Delta y) \\
&\quad \frac{\Delta x}{\Delta y} \\
&\quad \frac{\nabla \cdot \nabla I'}{\Delta A} \\
&\quad \frac{\nabla I'(x,y)}{\Delta A} \\
&\quad \frac{\nabla \cdot \nabla I'}{\Delta A}
\end{align*}$$

$\Phi_v = \frac{\nabla V \cdot dS}{\Delta A}$

$$\int \nabla \cdot \nabla I' \frac{\Delta A}{V} \approx \sum_i \sum \frac{\nabla \cdot \nabla I'}{\Delta A}$$

$$\frac{\Phi_v}{V} \approx \frac{\sum \frac{\nabla \cdot \nabla I'}{\Delta A}}{V}$$
Figure 1 Visualization and pixel processing sequence of a DCE-MRI breast tumor slice. DCE-MRI scan of patient with breast cancer viewed in three orientations (A); focused 2D image displaying an axial slice of tumor (B) with superimposed blue background for regional recognition and processing (C); tumor recognition values without digital mature vessel filtration (D) and with (E) comprising a numerical data matrix representative of the image pixels, displayed from a much zoomed out perspective elucidating the processed tumor values (miniscule font series of “1”) contrasting the null (miniscule font series of “0”). DCE-MRI, dynamic contrast enhanced magnetic resonance imaging; 2D, 2-dimensional.
Statistical analysis and validation

Analyses for correlations between the radiologically derived quantities, as well as axillary nodal markers were conducted using Pearson and Spearman correlation coefficients. Cross-correlations amongst the radiologic and remaining pathological data were computed in excluding potential confounders. Multivariable linear regression was analyzed in both step-wise and forced inclusion fashions for known prognostic determinants: age, body mass index (BMI), tumor size, and tumor grade. Similarly, partial correlation coefficients controlling for the effects of these prognostic determinants were derived. A two-tailed P-value of 0.05 was applied as a standard of significance. All analyses were performed using SPSS Statistics® software (version 22; IBM Corporation, Armonk, NY, USA) and plots generated using Excel™ software (version 14.0; Microsoft Corporation, Redmon, WA, USA).

Statistical validation was procured through cross-validation partitioning of the data into training and test sets respectively. Leave-one-out (LOO) techniques were utilized in completely permuting a single member test set through training sets constructed via a linear regression of the withheld members. Predictive capabilities were quantitated using mean squared error and interval normalized root mean square deviation (NRMSD). The code script was composed and compiled using Mathematica™ software.

Results

Patient nodal pathological status

All patients were subject to lymph node assessment through either sentinel node biopsy, axillary node dissection, or both (16 patients with both). Thirty-four patients underwent sentinel lymph node dissections (18 alone without further axillary node dissection) with a median of three nodes collected. These were positive in 14 patients ranging from 1 to 4 nodes. Axillary lymph nodes were completely dissected in a total of 29 patients (13 alone without prior sentinel node biopsy) with a median of 15 nodes collected. Twelve patients returned dissections pathologically negative for metastatic spread (Table 2).

The degree of total axillary nodes positive to number dissected (TN Ratio) exhibited a median of 0.04 in all patients; range 0 to 1.00, and a median of 0.14 in nodal-positive patients; range 0.03 to 1.00. The degree of non-sentinel axillary nodes positive to number dissected (AN Ratio) exhibited a median of 0.06 in all patients; range 0 to 1.00, and a median of 0.14 in nodal-positive patients; range 0.03 to 1.00. The degree of sentinel nodes positive to number dissected exhibited a median of 0 in all patients; range 0 to 1.00, and a median of 0.50 in nodal-positive patients; range 0.20 to 1.00.

Radiological analysis

MRI sequence analysis and calculations demonstrated a mean contoured tumor volume of 6.32 cm$^3$; range 0.26 to 32.34 cm$^3$. The sum of VIG divergence exhibited a mean value of 84.06 in all patients; range -8.89 to 966.49. The normalized values, representative of the 2D heterogeneity flux, displayed a mean of 9.39 in all patients; range -13.89 to 51.01. In nodal-positive patients, this normalized 2D heterogeneity flux displayed a mean of 11.40 with an identical range. In patients having undergone axillary dissection, this mean is 10.36 and 11.38 for all patients and nodal-positive patients respectively with ranges identical to the cohort.

Normalized 2D VIG divergence correlations

In all patients, the normalized 2D heterogeneity flux (hereby labeled “flux”) was observed to significantly correlate with the TN Ratio and AN Ratio. The Pearson correlation coefficient between flux and TN ratio (Figure 2A) is 0.50 (P<0.001) and AN Ratio...
Table 1  Patient demographics and respective tumor pathologic data

<table>
<thead>
<tr>
<th>Clinical variable (N=47)</th>
<th>T1 tumor (N=33)</th>
<th>T2 tumor (N=14)</th>
<th>P-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mean age (years ± SD)</td>
<td>57.7±10.6</td>
<td>54.2±8.8</td>
<td>0.26</td>
</tr>
<tr>
<td>Mean greatest tumor diameter (cm ± SD)</td>
<td>1.02±0.48</td>
<td>3.1±0.86</td>
<td>&lt;0.001</td>
</tr>
<tr>
<td>Menopause No. (%)</td>
<td></td>
<td></td>
<td>0.96</td>
</tr>
<tr>
<td>Pre</td>
<td>6 (18.2)</td>
<td>2 (14.3)</td>
<td></td>
</tr>
<tr>
<td>Post</td>
<td>20 (60.6)</td>
<td>7 (50.0)</td>
<td></td>
</tr>
<tr>
<td>Missing</td>
<td>7 (21.2)</td>
<td>5 (35.7)</td>
<td></td>
</tr>
<tr>
<td>Tumor histology No. (%)</td>
<td></td>
<td></td>
<td>0.45</td>
</tr>
<tr>
<td>Invasive ductal carcinoma</td>
<td>29 (87.9)</td>
<td>13 (92.9)</td>
<td></td>
</tr>
<tr>
<td>Invasive lobular carcinoma</td>
<td>3 (9.1)</td>
<td>1 (7.1)</td>
<td></td>
</tr>
<tr>
<td>Other</td>
<td>1 (3.0)</td>
<td>0 (0.0)</td>
<td></td>
</tr>
<tr>
<td>Nuclear grade No. (%)</td>
<td></td>
<td></td>
<td>0.22</td>
</tr>
<tr>
<td>1</td>
<td>8 (24.2)</td>
<td>2 (14.3)</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>13 (39.4)</td>
<td>4 (28.6)</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>12 (36.4)</td>
<td>8 (57.1)</td>
<td></td>
</tr>
<tr>
<td>Lymphovascular invasion No. (%)</td>
<td></td>
<td></td>
<td>0.003</td>
</tr>
<tr>
<td>No</td>
<td>31 (93.9)</td>
<td>6 (42.9)</td>
<td></td>
</tr>
<tr>
<td>Yes</td>
<td>2 (6.1)</td>
<td>8 (57.1)</td>
<td></td>
</tr>
<tr>
<td>Extracapsular extension No. (%)</td>
<td></td>
<td></td>
<td>0.02</td>
</tr>
<tr>
<td>No</td>
<td>33 (100.0)</td>
<td>9 (64.3)</td>
<td></td>
</tr>
<tr>
<td>Yes</td>
<td>0 (0.0)</td>
<td>5 (35.7)</td>
<td></td>
</tr>
<tr>
<td>ER No. (%)</td>
<td></td>
<td></td>
<td>0.50</td>
</tr>
<tr>
<td>Negative</td>
<td>6 (18.8)</td>
<td>4 (28.6)</td>
<td></td>
</tr>
<tr>
<td>Positive</td>
<td>26 (81.2)</td>
<td>10 (71.4)</td>
<td></td>
</tr>
<tr>
<td>PR No. (%)</td>
<td></td>
<td></td>
<td>0.91</td>
</tr>
<tr>
<td>Negative</td>
<td>12 (37.5)</td>
<td>5 (35.7)</td>
<td></td>
</tr>
<tr>
<td>Positive</td>
<td>20 (62.5)</td>
<td>9 (64.3)</td>
<td></td>
</tr>
<tr>
<td>HER2 No. (%)</td>
<td></td>
<td></td>
<td>0.54</td>
</tr>
<tr>
<td>Negative</td>
<td>25 (78.1)</td>
<td>12 (85.7)</td>
<td></td>
</tr>
<tr>
<td>Positive</td>
<td>7 (21.9)</td>
<td>2 (14.3)</td>
<td></td>
</tr>
<tr>
<td>Triple negative No. (%)</td>
<td></td>
<td></td>
<td>0.50</td>
</tr>
<tr>
<td></td>
<td>6 (18.8)</td>
<td>4 (28.6)</td>
<td></td>
</tr>
</tbody>
</table>

ER, estrogen receptor; PR, progesterone receptor; HER2, human epidermal growth factor receptor 2.

(Figure 2B) is 0.57 (P=0.001). After adjusting for age, BMI, tumor size, and grade, Pearson correlation coefficient (i.e., partial correlation) is 0.45 (P=0.003) and 0.51 (P=0.009) for TN Ratio and AN Ratio respectively. These relationships were substantially augmented in nodal-positive patients (AN/TN Ratio ≠0). In such patients, Pearson correlation coefficient between flux and TN ratio (Figure 2C) is 0.58 (P=0.002) and AN Ratio (Figure 2D) is 0.72 (P=0.001).
The adjusted partial coefficients are 0.60 (P=0.003) and 0.60 (P=0.032) for nodal-positive TN Ratio and AN Ratio respectively.

**Statistical validation**

These significant results were further justified through LOO cross validation studies. Mean squared error for all AN Ratio and TN Ratio was 0.048 (NRMSD =0.22) and 0.036 (NRMSD =0.19) respectively. For nodal-positive patients, these mean squared errors were 0.049 (NRMSD =0.23) and 0.045 (NRMSD =0.22) respectively.

**Multivariable analysis**

The normalized 2D heterogeneity flux was only further detected to significantly correlate with patient age via Pearson coefficient of 0.32 (P=0.027). Patient age also displayed significant correlation with AN Ratio in nodal-positive patients with coefficient of 0.51 (P=0.036). However, forced inclusion multivariable linear regression in this subgroup yielded no significant relationship between age and AN Ratio with a partial coefficient of 0.23 (P=0.45) in light of including flux. In fact, step-wise multivariable linear regression exclusively incorporated flux as the sole significant independent determinant of all nodal ratios. The standardized beta regression coefficient for flux was 0.469 (P=0.003) and 0.562 (P=0.009) in the case of TN Ratio and AN Ratio respectively. In nodal-positive patients, this regression coefficient for flux was 0.711 (P=0.003) and 0.602 (P=0.032) for TN Ratio and AN Ratio respectively. The flux was not found to significantly cross-correlate with other clinically relevant markers. Similarly, each clinical marker including the AN Ratio and TN Ratio demonstrated no significant cross-correlation with the remaining pathological features analyzed.

**Discussion**

**Heterogeneity flux pertinence and mechanism**

To our knowledge, our study is the first in radiologically investigating 2D breast tumor heterogeneity flux through the divergence theorem via summation of VIG divergence. In particular, our analysis focused on ascertaining potential correlations to pathologically acquired axillary prognostic markers. Axillary nodal measures demonstrated several statistically significant correlations. Both the TN Ratio and AN Ratio with significantly linked with 2D heterogeneity flux across all patients evaluated. Further assessment of such correlations in nodal-positive subgroups of patients yielded emphatically improved Pearson coefficient results.

The observed outcomes of our methodology lend a degree of justification to its underlying premise. In formulating an algorithm for calculating the total VIG divergence encompassed in a tumor, we intended on deriving information regarding the normalized VIG flux at its surface. Such flux quantifies an intrinsic emanation portrayed by tumor components as cells and vessels. In light of this fundamental principle, the involvement of extra-tumor features as distant nodal status is mechanistically merited by elevated values of surface flux. It is interesting to contrast intra-tumor pathological markers as size, grade, receptor status and lymphovascular invasion which were not found to significantly correlate with flux.

As is the case with any clinical study, our methodologies and results may be subject to biases and flaws precluding perfect generalization. The number of patients analyzed in retrospective fashion is modest. Although all patients displayed axillary nodal evaluation, which significantly correlated with the flux in terms of positivity, the route of assessment was not uniform. 3-dimensional volumetric analyses were reduced to a series of 2D slice analyses secondary to a pre-determined sampling rate constraint adhered to by the MRI modality. Thus, solely flux exclusively tangential to the acquired transverse slides was subject to investigation using our 2D application of the divergence theorem. Although accurately capable of ascertaining the flux emanating through transverse surface boundaries, our methodology is susceptible to improvement in detecting flux possessing orthogonal components to

<table>
<thead>
<tr>
<th>Treatment modality</th>
<th>No. patients (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Radiation therapy</td>
<td>47 (100.0)</td>
</tr>
<tr>
<td>Total axillary management</td>
<td>47 (100.0)</td>
</tr>
<tr>
<td>Sentinel nodes obtained</td>
<td>34 (72.3)</td>
</tr>
<tr>
<td>Sentinel nodal positivity</td>
<td>14 (29.8)</td>
</tr>
<tr>
<td>Axillary lymph node dissection</td>
<td>29 (61.7)</td>
</tr>
<tr>
<td>Axillary lymph nodal positivity</td>
<td>17 (36.2)</td>
</tr>
<tr>
<td>Total axillary nodal positivity</td>
<td>26 (60.6)</td>
</tr>
</tbody>
</table>
Axial planes (z-directional). Correlation statistics utilized assume a degree of linearity to potential relationships. The true format of such relationships is not logically precluded from partial non-linear behavior and may not be perfectly represented via our chosen models.

**Clinical translation**

Throughout history, a consistent de-escalation to the surgical treatment of breast cancer is witnessed (31). Extensive national phase III trials have linked less aggressive operations to improved patient outcomes (32-34). Most currently, the ACOSOG Z0011 trial showed no survival difference in excluding certain groups of patients with positive sentinel nodes from undergoing an axillary lymph node dissection (35). As such, a lack of information pertaining to patients’ nodal disease may frequently be experienced in clinical cases. A potential conflict arises in light of...
the recently published results of the NCIC MA20 and EORTC 22922/10925 trials. These trials convergently demonstrated significant benefit in terms of decreased breast cancer recurrence rates, albeit sustaining the cost of additional adverse effects, with regional nodal irradiation (RNI) (23,24). This RNI was comprehensively administered to axillary, internal mammary, and supraclavicular lymph nodes. The MA20 study criteria accrued patients with confirmed nodal positivity or high nodal risk and mandated axillary lymph node dissection in all recruits (24). This generates an innate incongruence between the requirements and outcomes of these trails. A patient with inadequate lymph node sampling per Z11 may carry ambiguity in determining whether he/she would benefit from RNI per MA20. Complementary information provided via non-invasive radiogenomic methodologies may aid in optimally stratifying nodal-risk in lieu of pathological assessment. Personalized clinical decisions for administering RNI would thus be enhanced in accounting for results pertaining to axillary nodal status utilizing the 2D heterogeneity flux in early stage breast cancers.

Conclusions

In conclusion, our work introduces the quantity of tumor heterogeneity flux, a novel radiological variable capable of characterizing tumor environment. Being a static measure of intensity gradient emanating from the structural surface, such flux may correlate with a worse prognosis as manifested by axillary nodal involvement in early stage breast cancer. This correlation is optimally displayed in patients with nodal positivity. Our approach can be incorporated into future prognostic indices (nomograms) aimed at helping clinicians with axillary risk assessment.

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Footnote

Conflicts of Interest: The authors have no conflicts of interest to declare.

Ethical Statement: The authors declare that the methodology used in the ascertainment and analysis of data in this manuscript complies with the current laws in the United States. All procedures performed in studies involving human participants were in accordance with the ethical standards of the institutional and/or nation research committee and with the 1964 Helsinki declaration and its later amendments or comparable ethical standards. For this type of study formal consent is not required. Informed consent was obtained from all individual participants included in the study.

References
